

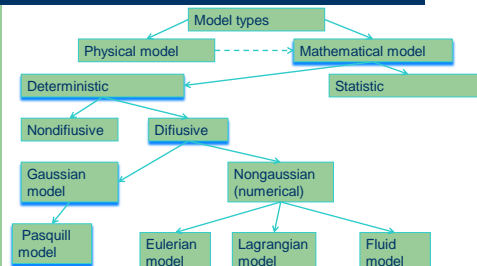
## Emission and Transport of Air Pollutants

### Lecture 7

**Model Pasquilla.**  
**Programmes for**  
**emission calculation.**  
**Low emission.**

1

## Modelling of the air pollution dispersion



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## Gaussian model – equation of turbulent diffusion – derivative form of mass principle conservation

$$\frac{\partial C}{\partial t} = -V \cdot \nabla C - \nabla \cdot F_e + Q + R$$

where: C – pollutant concentration, kg/m<sup>3</sup>

t – time, s

V – wind velocity vector, m/s

F<sub>e</sub> – turbulent mass stream of pollutant, kg/m<sup>2</sup>s

Q – emission capacity, kg/m<sup>3</sup>s

R – dry and wet deposition and chemical conversion  
of pollutant, kg/m<sup>3</sup>s

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## Equation of turbulent diffusion - equation of advective diffusion

$$\frac{\partial C}{\partial t} = -V \cdot \nabla C - \nabla \cdot F_e + Q + R$$

$$\frac{\partial C}{\partial t} = - \underbrace{\left( u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} + w \frac{\partial C}{\partial z} \right)}_{\text{advective term}} + \underbrace{\left( \frac{\partial}{\partial x} K_h \frac{\partial C}{\partial x} + \frac{\partial}{\partial y} K_h \frac{\partial C}{\partial y} + \frac{\partial}{\partial z} K_v \frac{\partial C}{\partial z} \right)}_{\text{diffusive term}} + \underbrace{Q + R}_{\text{middle term}}$$

where:

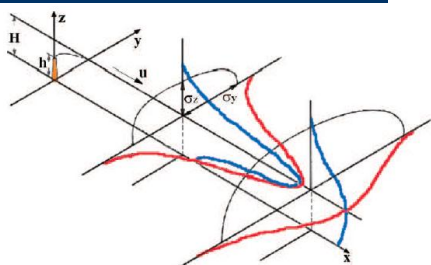
u, v, w – components of wind velocity,

K<sub>h</sub> = K<sub>xx</sub> = K<sub>yy</sub> and K<sub>v</sub> = K<sub>zz</sub>

K<sub>h</sub>, K<sub>v</sub> – vertical and horizontal turbulent diffusion  
coefficient

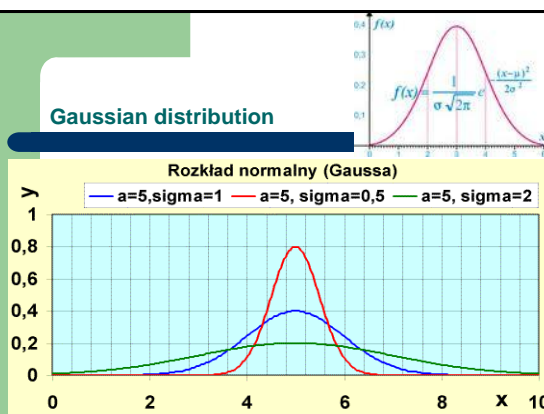
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## Gaussian model of pollutants dispersion in the atmosphere



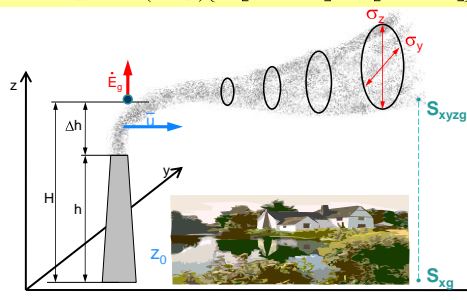
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## Gaussian distribution



### Gaussian plume model of pollutants dispersion in the atmosphere and Pasquill formula for gases

$$S_{xyzg} = \frac{\dot{E}_g}{2\pi \cdot \bar{u} \cdot \sigma_y \cdot \sigma_z} \exp\left(-\frac{y^2}{2\sigma_y^2}\right) \left\{ \exp\left[-\frac{(z-H)^2}{2\sigma_z^2}\right] + \exp\left[-\frac{(z+H)^2}{2\sigma_z^2}\right] \right\} \cdot 1000$$



### Pasquill formula of pollutants dispersion in the atmosphere

$$S_{xyzg} = \frac{\dot{E}_g}{2\pi \cdot \bar{u} \cdot \sigma_y \cdot \sigma_z} \exp\left(-\frac{y^2}{2\sigma_y^2}\right) \left\{ \exp\left[-\frac{(z-H)^2}{2\sigma_z^2}\right] + \exp\left[-\frac{(z+H)^2}{2\sigma_z^2}\right] \right\} \cdot 1000$$

where:

$S_{xyzg}$  – gas pollutant concentration at the receptor point,  $\mu\text{g}/\text{m}^3$

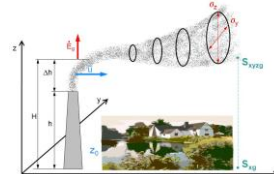
$\dot{E}_g$  – emission of gas substance from source situated in point  $x_0=y_0=0$ ,  $z_0=H$ ,  $\text{mg}/\text{s}$

$\sigma_y, \sigma_z$  – horizontal and vertical diffusion coefficient, m

$\bar{u}$  – average wind velocity in layer: from h to H, m/s

x, y, z – coordinate of receptor point, for which concentration of substances in air is calculated, m

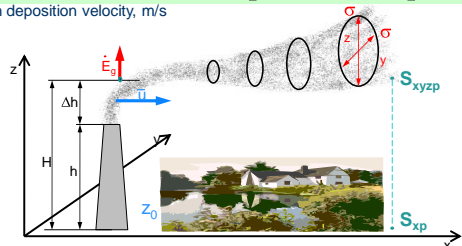
H – effective high of emission source, m



### Gaussian plume model of pollutants dispersion in the atmosphere and Pasquill formula for fly ash

$$S_{xyzp} = \frac{\dot{E}_p}{2\pi \cdot \bar{u} \cdot \sigma_y \cdot \sigma_z} \exp\left(-\frac{y^2}{2\sigma_y^2}\right) \exp\left[-\frac{\left(z-H-w_f \frac{x}{\bar{u}}\right)^2}{2\sigma_z^2}\right] \cdot 1000$$

$w_f$  – ash deposition velocity, m/s



### Pasquill formula for pollution dispersion on surface of terrain in wind axes and distance x from emission source

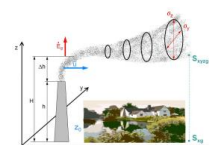
$$S_{xg} = \frac{\dot{E}_g}{\pi \cdot \bar{u} \cdot \sigma_y \cdot \sigma_z} \exp\left(-\frac{H^2}{2\sigma_z^2}\right) 1000$$

gdzie:

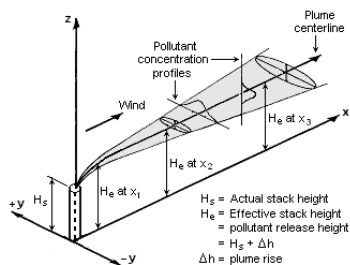
$S_{xg}$  – gas pollutant concentration,  $\mu\text{g}/\text{m}^3$ , for  $y=z=0$

$$S_{xp} = \frac{\dot{E}_p}{2 \cdot \pi \cdot \bar{u} \cdot \sigma_y \cdot \sigma_z} \exp\left(-\frac{H^2}{2\sigma_z^2}\right) 1000$$

$S_{xp}$  – fly ash concentration,  $\mu\text{g}/\text{m}^3$ , for  $y=z=0$  and ash deposition velocity  $w_f=0$



### Gaussian plume model of pollutants dispersion in the atmosphere



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### Diffusion coefficient (Dz.U. nr 16 poz. 67)

Horizontal diffusion coefficient, m

$$\sigma_y = A \cdot x^a$$

Vertical diffusion coefficient, m

$$\sigma_z = B \cdot x^b$$

$\sigma_y, \sigma_z$  – standard deviations of the pollutant concentration distribution

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### Coefficient A and B (Dz.U. nr 16 poz. 67)

$$A = 0,088 \left( 6m^{-0,3} + 1 - \ln \frac{H}{z_0} \right)$$

$$B = 0,38m^{1,3} \left( 8,7 - \ln \frac{H}{z_0} \right)$$

$$\frac{H}{z_0} = 10, \text{ when } \frac{H}{z_0} < 10$$

$$\frac{H}{z_0} = 1500, \text{ when } \frac{H}{z_0} > 1500$$

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### Coefficients (Dz.U. nr 16 poz. 67)

Tablica 2.2 Stałe zależne od stanów równowagi atmosfery

Stała	Stan równowagi atmosfery					
	1	2	3	4	5	6
<b>m</b>	0,080	0,143	0,196	0,270	0,363	0,440
<b>a</b>	0,888	0,865	0,845	0,818	0,784	0,756
<b>b</b>	1,284	1,108	0,978	0,822	0,660	0,551
<b>g</b>	1,692	1,781	1,864	1,995	2,188	2,372
<b>C<sub>1</sub></b>	0,213	0,218	0,224	0,234	0,251	0,271
<b>C<sub>2</sub></b>	0,815	0,771	0,727	0,657	0,553	0,457

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### Maximal concentration of pollutants in the air

Maximal concentration of **gas substance** in the air, and **suspended ash** for single source, averaged for **one hour** in **particular meteorological situation**:

$$S_{mg} = C_1 \frac{\dot{E}_g}{\bar{u} \cdot A \cdot B} \left( \frac{B}{H} \right)^g 1000$$

$$S_{mp} = C_1 \frac{\dot{E}_p}{2 \cdot \bar{u} \cdot A \cdot B} \left( \frac{B}{H} \right)^g 1000$$

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### Maximal concentration of pollutants in the air

$$S_{mg} = C_1 \frac{\dot{E}_g}{\bar{u} \cdot A \cdot B} \left( \frac{B}{H} \right)^g 1000 \quad S_{mp} = C_1 \frac{\dot{E}_p}{2 \cdot \bar{u} \cdot A \cdot B} \left( \frac{B}{H} \right)^g 1000$$

$S_{mg}$  - Maximal concentration of gas substance in the air, ,  $\mu\text{g}/\text{m}^3$

$S_{mp}$  - Maximal concentration of suspended ash in the air, ,  $\mu\text{g}/\text{m}^3$

$C_1, g$  - Constant coefficient depended on equilibrium state of atmosphere

$\dot{E}_g$  - Maximal emission of gas substances,  $\text{mg}/\text{s}$

$\dot{E}_p$  - Maximal emission of suspended ash,  $\text{mg}/\text{s}$

$\bar{u}$  - Average wind velocity in layer from h to H,  $\text{m}/\text{s}$

$A, B$  - Coefficient depended on m,  $z_0$ , H

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### Maximal concentration of pollutants in the air

**Distance from the source**, where concentration of pollutant, as well as ash, reaches **maximal value** for single source, averaged for **one hour** in **particular meteorological situation**.

$$x_m = C_2 \left( \frac{H}{B} \right)^{\frac{1}{b}}$$

$C_2, b$  - constant coefficient depended on equilibrium state of the atmosphere

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### Maximal concentration of pollutants in the air

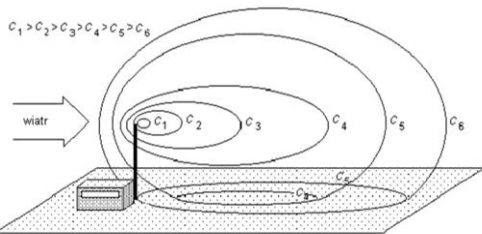
•  $S_m$  and  $S_{mp}$  value should be **calculated for 36 meteorological situations**

• From group of 36 values of  $S_m$  for each substance, the maximum value is chosen and denoted  $S_{mm}$ .

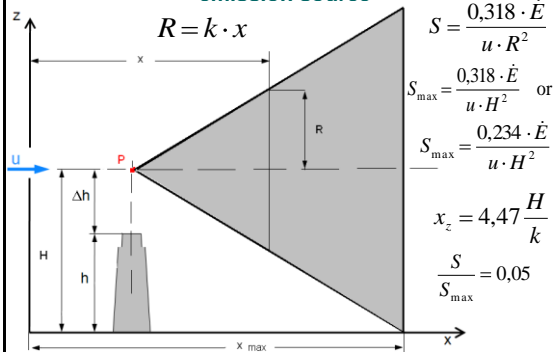
• Terrain of installation is excluded from area, where calculations are carried out.

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### Maximal concentration of pollutants in the air



### Simplified model of pollutants dispersion from point emission source



### Simplified model of pollutants dispersion from point emission source

$$R = k \cdot x$$

$$S = \frac{0,318 \cdot \dot{E}}{u \cdot R^2}$$

$$S_{\max} = \frac{0,318 \cdot \dot{E}}{u \cdot H^2} \quad \text{or} \quad S_{\max} = \frac{0,234 \cdot \dot{E}}{u \cdot H^2}$$

$$x_z = 4,47 \frac{H}{k}$$

$$\frac{S}{S_{\max}} = 0,05$$

R – radius of pollutant trail  
u – wind velocity on height H,  
k – atmosphere diffusion coefficient, (cross related to x direction)  
E – pollutant emission, kg  
H – effective source height,  
x<sub>z</sub> – range, where source P has effect on, where concentration drops to 5% of its maximal value

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### Data required to calculation

- Emission source parameters: height [m], outlet diameter [m], gas velocity at the outlet [m/s], gas temperature [K],
- Pollutants emission [kg/h],
- Background of substances [μg/m<sup>3</sup>]
- Ambient temperature [°C],
- Work period during the year [h],
- Shape of the area and roughness factor,
- Compass rose.

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### Pollutants backgrounds for installation in Kęty

Substance	Reference value in μg/m <sup>3</sup> averaged for period		Background [μg/m <sup>3</sup> ]	Notes
	1 hour	1 year		
1 Aceton	350	30	3	10% D <sub>s</sub>
2 Akrylaldehyd (akroleina)	10	0,9	0,09	10% D <sub>s</sub>
3 Cykloheksan	10	1	0,1	10% D <sub>s</sub>
4 Cykloheksanon	40	3,5	0,35	10% D <sub>s</sub>
5 Nitrogen dioxide	200	40	26	-
6 Sulphur dioxide	350	30	3	10% D <sub>s</sub>
7 Etylobenzen	500	38	3,8	10% D <sub>s</sub>
8 Alkohol dwuacetonowy	150	7,9	0,79	10% D <sub>s</sub>
9 Izocyjaniany	10	1,3	0,13	10% D <sub>s</sub>
10 Ksylen	100	10	1	10% D <sub>s</sub>
11 Alkohol izobutyłowy	300	26	2,6	10% D <sub>s</sub>
12 Octan butylu	100	8,7	0,87	10% D <sub>s</sub>
13 Octan etylu	100	8,7	0,87	10% D <sub>s</sub>
14 Suspended ash PM 10	280	40	30	-
15 Carbon monoxide	30000	-	-	-
16 Aliphatic hydrocarbones	3000	1000	100	10% D <sub>s</sub>
17 Aromatic hydrocarbones	1000	43	4,3	10% D <sub>s</sub>

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### Pollutants backgrounds for installation in Kęty

Contamination state of air described on the basis of information from Voivodeship Inspectorate of Environment Protection in Cracow, 22. 02. 2007

Tabela 2. Present air contamination state in Kęty

Substance	Annual average concentration [μg/m <sup>3</sup> ]	Permissible value [μg/m <sup>3</sup> ]	% of permissible value
Suspended ash PM 10	30	40	75
Nitrogen dioxide	26	40	65
Lead	0,04	0,5	8
Benzene	3,2	5	64

Quality of air in area around the installation is influenced by affecting industrial plants, roads, dust and pollutants emission from local sources (chimneys, boilers, etc.).

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## Programmes used to modelling of the air pollution dispersion

- Sozat – EK100 W / ATMOTERM
  - Komin / Rww / EcoSoft
  - Emitor / Obserwator imisji / Polstage
  - ISC 3
  - ZANAT
  - URFOR
- 
- COPERT
  - HBEFA (Niemiecki)
  - INRETS (Francuski)

For line source of emission

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## Programmes used to modelling of the air pollution dispersion

- CALMET/CALPUFF (California) – Lagrangian model
  - MISCAM
  - STEM II
  - RADM
  - GATOR
  - POLSOXNOX
  - HARWELL LABORATORY
  - AVACTA
  - ATSTEP
  - SPM
  - EMEP
  - RPM
- 
- RIMPUFF
  - ADPIC
  - ARCO
  - MDMS
  - CAR

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## „Emitor” Programme

### Program „Emitor”

„...twoje środowisko do modelowania rozprzestrzeniania zanieczyszczeń”



Polstage Sp. z o.o.  
44-292 Rybnik, ul. Gzelska 69

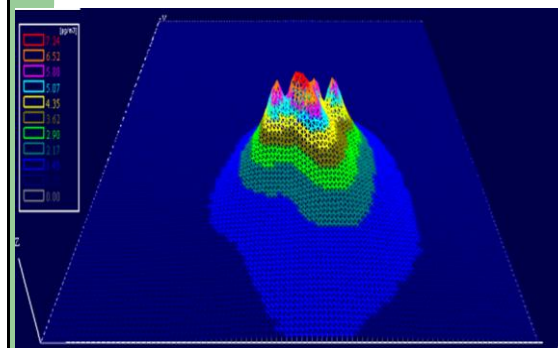
Biurowo: 44-100 Gliwice  
ul. Kościuszki 1  
tel. +48/32/330 56 60  
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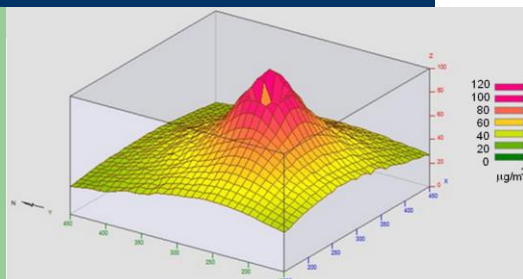
e-mail: office@polstage.pl  
http://www.polstage.pl

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## „Obserwator imisji” – isoline of concentration

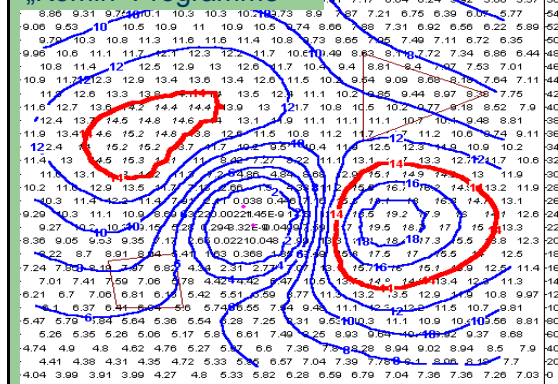


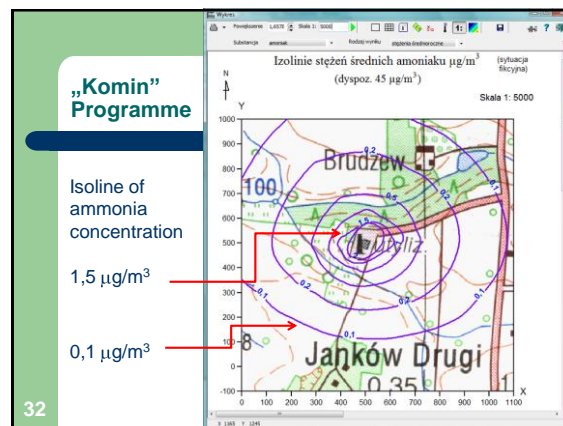
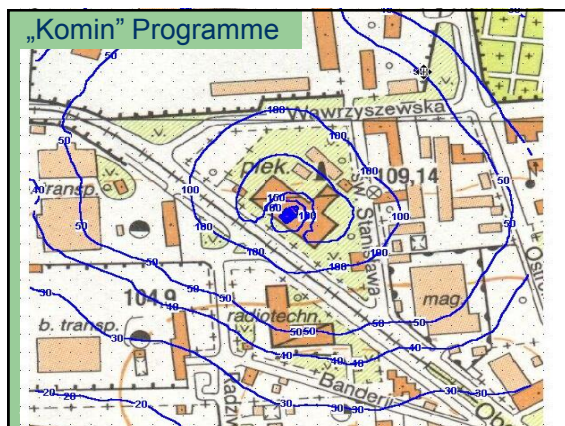
## „Komin” Programme Isoline of maximal concentration of sulfur dioxide, $\mu\text{g}/\text{m}^3$



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## „Komin” Programme





**COPERT software**

COPERT is model and programme to determination of air pollution from transport means

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**EK-100W software contained in SOZAT package**

**ATMOTERM® S.A.**  
Wszystkie prawa zastrzeżone

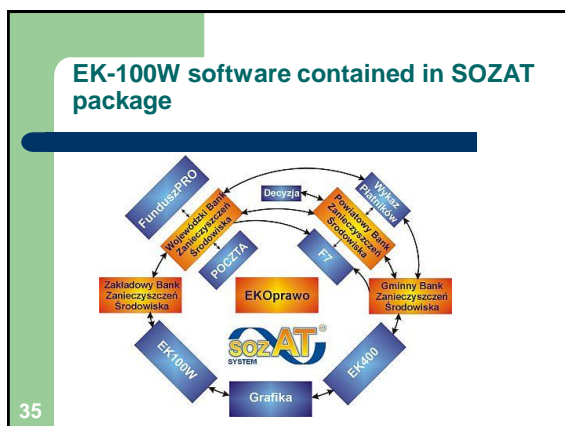
ATMOTERM S.A.  
ul. Łągowiejskiego 4  
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tel. 77 / 44 11 557  
77 / 44 11 578  
fax 77 / 44 26 695

office@atmoterm.pl  
www.atmoterm.pl

**EK100W**

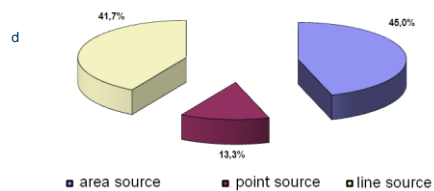
wer. 4.6



**TABL.5(140). CAŁKOWITA EMISJA DWUTLENKU SIARKI, TLENKÓW AZOTU I PYŁÓW**  
**TOTAL EMISSIONS OF SULPHUR DIOXIDE, NITROGEN OXIDES AND PARTICULATES**

WYSZCZEGÓLNIENIE	2000	2005	2007	2008	SPECIFICATION
w giganach					
<b>DWUTLENEK SIARKI</b> <b>SULPHUR DIOXIDE</b>					
<b>O G Ó Ł E M.....</b>	<b>1511</b>	<b>1222</b>	<b>1216</b>	<b>990</b>	<b>TOTAL</b>
Energetyka zawodowa .....	805	873	684	448	Power generating plants
Energetyka przemysłowa .....	265	202	200	192	Industrial power plants
Technologie przemysłowe .....	91	56	25	24	Industrial technologies
Inne źródła stacjonarne <sup>a</sup> .....	309	290	324	333	Other stationary sources <sup>a</sup>
Źródła mobilne.....	41	1 <sup>1</sup>	2 <sup>2</sup>	2 <sup>2</sup>	Mobile sources
<b>TLENKI AZOTU<sup>b</sup></b> <b>NITROGEN OXIDES<sup>b</sup></b>					
<b>O G Ó Ł E M.....</b>	<b>838</b>	<b>811</b>	<b>800</b>	<b>831</b>	<b>TOTAL</b>
Energetyka zawodowa .....	237	246	247	226	Power generating plants
Energetyka przemysłowa .....	93	125	96	84	Industrial power plants
Technologie przemysłowe .....	75	54	51	48	Industrial technologies
Inne źródła stacjonarne <sup>a</sup> .....	120	74	118	122	Other stationary sources <sup>a</sup>
Źródła mobilne.....	313	312	349	350	Mobile sources
<b>PYŁY</b> <b>PARTICULATES</b>					
<b>O G Ó Ł E M.....</b>	<b>464</b>	<b>430</b>	<b>430</b>	<b>421</b>	<b>TOTAL</b>
Energetyka zawodowa .....	64	39	38	24	Power generating plants
Energetyka przemysłowa .....	19	13	12	9	Industrial power plants
Technologie przemysłowe .....	72	53	62	58	Industrial technologies
Inne źródła stacjonarne <sup>a</sup> .....	248	257	243	249	Other stationary sources <sup>a</sup>
Źródła mobilne.....	61	68	77	82	Mobile sources

### Contribution of sources in PM<sub>10</sub> emission (Białystok)



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### PAH emission depending on organization of combustion process

Fuel	Application	BaP emission index, mg/GJ
Hard coal	Pulverised coal boilers	0,47
	Boilers with mechanical stoker	1,9-152
	Local small boilers	188
	Household furnace	910
Oil	Household furnace	0,28-560
Natural gas	Household furnace	0,019
Petrol	Motor vehicle	0,57
Disel oil	Motor vehicle	2,18

### Exam questions

1. What is Pasquill model used for?
2. What parameters influence diffusion coefficient of the atmosphere  $\sigma_y$ ,  $\sigma_z$ ?
3. Draw pollutant dispersion model.
4. Enumerate three programmes for air pollution dispersion modelling.
5. What is isoline of concentration? Explain by drawing.
6. For which substances, when and why pollutant background in urban agglomeration in Poland is higher than  $0,1D_s$ ?

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